1

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- But also presence of water drops decreases breakdown field:
 1.4 mm diameter water drops leads to E_{break} = 10 kV/cm



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- In mature thunderclouds minimum field to have corona streamers

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 Table 3.2. Maximum electric field magnitudes measured

 in thunderclouds

Reference	Sounding type	Maximum electric field, V m ⁻¹
Gunn (1948) Imyanitov et al. (1971) Winn et al. (1974) Winn et al. (1981) Weber et al. (1982) Byrne et al. (1983) Fitzgerald (1984) Marshall and Rust (1991) Kasemir (as reported by MacGorman and Rust 1998)	Aircraft Aircraft Rockets Balloons Balloons Aircraft Balloons Aircraft	$\begin{array}{c} 3.4\times10^5\\ 2.8\times10^5\\ 4\times10^5\\ 1.4\times10^5\\ 1.1\times10^5\\ 1.3\times10^5\\ 1.2\times10^5\\ 1.5\times10^5\\ 3\times10^5\end{array}$

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MacGorman and Rust 1998)			

- Breakdown field at sea level: E_{break} = 30 kV/cm
- At 6 km: E_{break} = 16 kV/cm \rightarrow Paschen law

- **BUT**: maybe some very strong field locally and short live
- We might hear more about that in later talks about runaway electrons

• $0.9 \cdot 5 \cdot 10^5 \text{ C/}$

•
$$0.9 \cdot 5 \cdot 10^5 \text{ C/}\left(\frac{4}{3}\pi\left(\left[R_{\text{Earth}} + 5 \text{ km}\right]^3 - R_{\text{Earth}}^3\right)\right)$$

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- Mean charge density is $\sim 30 \text{ nC/m}^3$ (x 150'000 increase)
- ~ 0.3 3 nC/m³. Locally can go up to 100 nC/m³

Cloud electrification mechanism: Convection



Cloud electrification mechanism: Convection



Remember: Fair-weather space charge: $\sim 0.2 \text{ pC/m}^3$

Cloud electrification mechanism: Convection



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 $0.25 \text{ fC} \simeq 1560 \text{ e}$





 $0.25 \text{ fC} \simeq 1560 \text{ e}$



- Origin of sign depends on many factors (temperature, cloud water content, ice criystal size, relative velocity,).
- Thought to be correlated to ice and graupel surface growth No consensus on physical details.
- Still this is the priviledged theory since

Charge density of precipitation ~ charge density inferred from E-field

Lightning representation in numerical cloud models

 Most model make crude assumptions but still show some reasonable values for charge per unit lightning length, total charge transfer and dipole moment charge.

Lightning representation in numerical cloud models

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 - Either slab-symmetric or axi-symmetric to reduce dimensionality
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 - Lightning staring always at same grid point with max E field value
 - Graupel-ice mechanism as electrification

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Lightning representation in numerical cloud models

- Most model make crude assumptions but still show some reasonable values for charge per unit lightning length, total charge transfer and dipole moment charge.
 - Either slab-symmetric or axi-symmetric to reduce dimensionality
 - Hard threshold of ~ 1-4 kV/cm is set to initiate lightning
 - Lightning staring always at same grid point with max E field value
 - Graupel-ice mechanism as electrification
 - ...
 - Even refined versions still lack fundamental limits: eg. Lightning initiation criterion still remains an open question.

Table 3.3. Median and maximum measured values of $|E_z|$ in various types of stratiform clouds. Adapted from Imyanitov et al. (1971)

Median value of $ E_z $, V m ⁻¹			
St Petersburg, Russia (60° N)	Kiev, Ukraine (50° N)	Tashkent, Uzbekistan (41° N)	Maximum measured value of $ E_z $, V m ⁻¹
100	120	130	$(2-3) \times 10^3$
80	100	100	$(2-3) \times 10^3$
40	80	70	5×10^{3}
100	150	350	2×10^{4}
150	250	500	4×10^{4}
	Median St Petersburg, Russia (60° N) 100 80 40 100 150	Median value of $ E_z $, V St Petersburg, Russia (60° N) Kiev, Ukraine (50° N) 100 120 80 100 40 80 100 150 150 250	Median value of $ E_z $, V m ⁻¹ Median value of $ E_z $, V m ⁻¹ Tashkent, Uzbekistan (41° N) 100 120 130 80 100 100 40 80 70 100 150 350 150 250 500

Table 3.4. Average thickness (m) of various types of stratiform cloud. Adapted from Imyanitov et al. (1971)

Type of cloud	Single charge layer		Two charge layers		Multiple
	÷	_	±	Ŧ	charge layers
St	200	200	450	450	700
Sc	260	250	400	450	700
As	650	700	800	900	1500
Ns	650	700	950	1600	2000





